

AMSC/CMSC 460: HW #8
Due: Tuesday 4/4/17 (in class)

Please submit the solution to at least one problem in LaTeX.

1. Use the Gram-Schmidt process to construct the first three orthonormal polynomials for the following intervals (all with weight $w(x) = 1$): (a) $[0, 1]$. (b) $[-1, 3]$. (c) $[-1, 1]$.
2. Find the linear least squares polynomial approximation to $f(x)$ in the indicated interval if
 - (a) $f(x) = x^3 + 3x + 2$ on $[0, 1]$
 - (b) $f(x) = \frac{1}{2} \cos x + \frac{1}{3} \sin 2x$ on $[-1, 1]$
3. Find the least squares polynomial approximations of degree two to the functions and intervals in the previous problem.
4. Find the first two orthonormal polynomials (polynomials of degree 0 and degree 1) for the following weight functions $w(x)$ on the indicated intervals $[a, b]$:
 - (a) $w(x) = \ln(x)$, $0 \leq x \leq 1$.
 - (b) $w(x) = x$, $0 \leq x \leq 1$.
 - (c) $w(x) = \sqrt{1 - x^2}$, $-1 \leq x \leq 1$.