Basic Properties of Probability.

1. List sample spaces for the following experiments

(a) A coin is tossed once;

- (b) A coin is tossed twice;
- (c) A number of power outages at a house during a summer is recorded;
- (d) A lifetime of a light bulb is observed;
- (e) A random STAT400 student is chosen and his final grade is recorded.

2. (a) Bob owns 3 bottles of wine: a Merlot, a Cabernet Sauvignon and a Pinot Noir. He has to serve one bottle during the dinner. List the sample space.

(b) Alice owns 4 bottles of wine: a Riesling, a Chardonnay, a Sauvignon Blanc and a Pinot Grigio. She has to serve one bottle during the dinner. List the sample space.

(c) Alice and Bob contribute one bottle each for the dinner. List the sample space.

3. A coin is tossed three times. Let $A = \{$ first head $\}, B = \{$ even number of heads $\}, C = \{$ second tail $\}.$

(a) List outcomes in A, B and C.

(b) Compute $A \cup B$, $A \cap B$, $A \cap C$, A^c .

4. A coin is called fair if P(H) = P(T).

(a) Compute P(H) for a fair coin.

(b) A fair coin is tossed repeatedly until a head comes. Find the probability that more than 1 toss is needed.

5. At Books, etc. store 60 % of the customers buy books, 40 % buy CDs and 20 % buy both books and CDs. What percentage of people buy at least one of those products? exactly one?

6. 50 % of students at Lazy College take at least 5 courses per semester 70 % have evening jobs, and 90 % either take at least 5 courses or work in the evening. How many students do both?

7. In a certain town 40 % of men are watching football, 35 % are watching baseball, 40 % are watching basketball, 15 % watch both football and baseball, 15 % watch both football and basketball, 20 % watch both baseball and basketball and 10 % watch all three sports. What per cent of the population watch exactly 2 sports?

8. 59 % cars of certain car model come with cruise control, 49 % have sunroof, 15 % have built-in phone, 84 % have either cruise control or sunroof, 65 % have either cruise control or phone, 55 % have either sunroof of phone and 85 % have at least one gadget these gadgets. How many cars have exactly one of these options?

9. A die is rolled 2 times. What is a more likely outcome for the sum of the rolls 9 or 10?